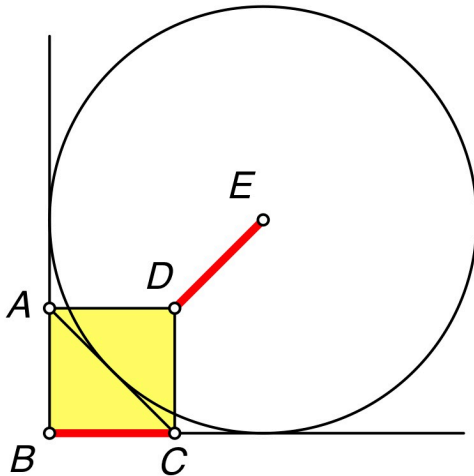


ABCD is a square.

$I = \text{incenter}(\triangle ABC)$

Prove: $BC=DI$

Stanley Rabinowitz, December, 2019

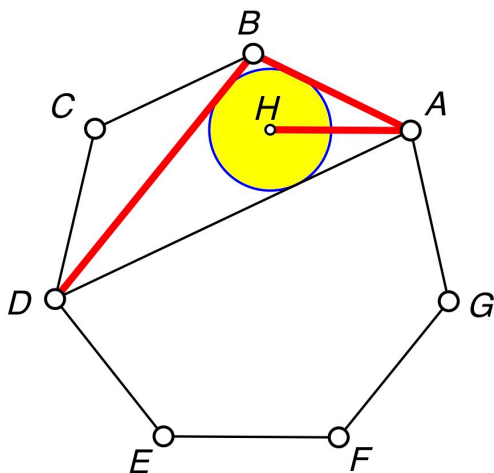


ABCD is a square.

E is center of excircle of $\triangle ABC$ tangent to AC .

Prove: $BC=DE$

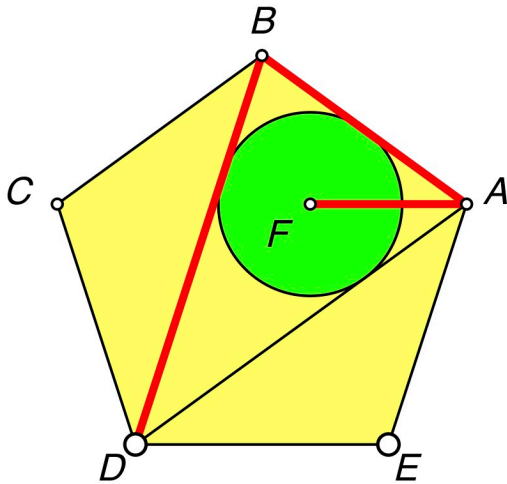
Stanley Rabinowitz, December 2019



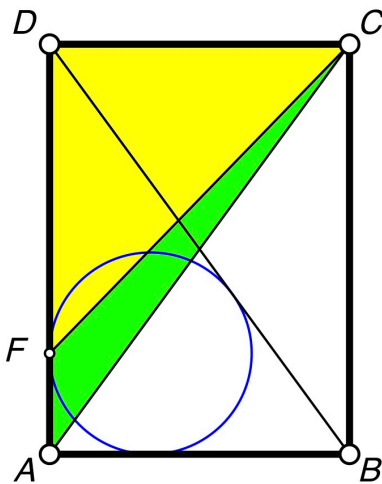
ABCDEFG is a regular heptagon.
 H is the incenter of $\triangle ABD$.

Prove: $HA+AB=BD$

Stanley Rabinowitz, December 2019



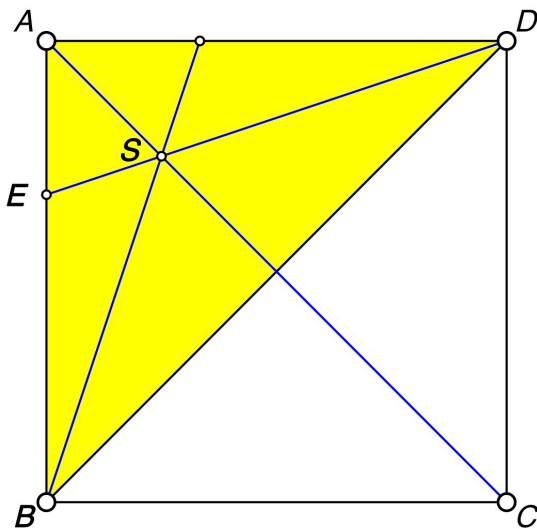
ABCDE regular pentagon
 1. $F = \text{incenter}[ABD]$
 Conclusion: $FA + AB = BD$



ABCD is a rectangle.
 The incircle of $\triangle ABD$ touches AD at F.

Prove: $\triangle FDC$ and $\triangle ACF$ have the same perimeter.

Stanley Rabinowitz, December 2019

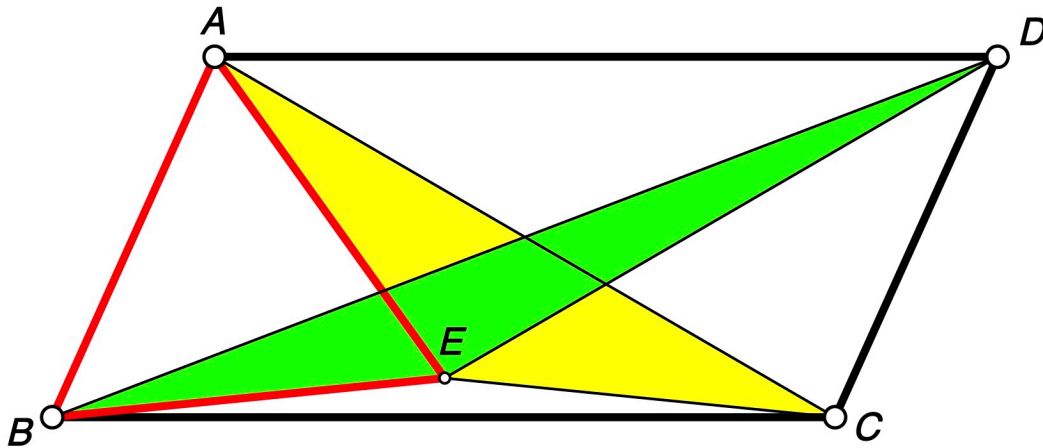


ABCD is a square.
 S is the symmedian point of $\triangle ABD$.

Prove:

- (i) $AB = 3AE$
- (ii) $DS = 3SE$
- (iii) $\triangle AES \sim \triangle CBS$

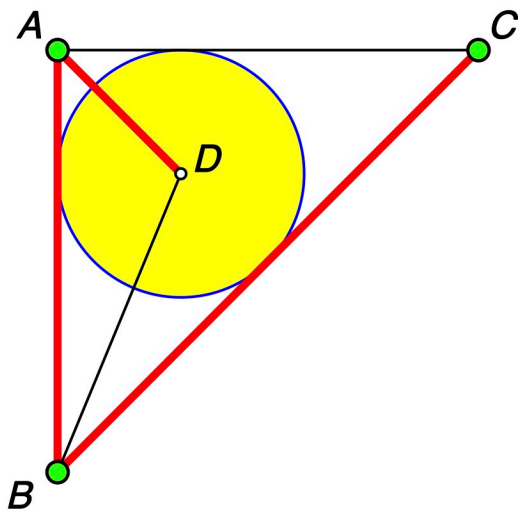
Stanley Rabinowitz, December 2019



ABCD is a parallelogram.
 ABE is an equilateral triangle.

Prove: $\triangle ACE$ and $\triangle BDE$ have the same centroid.

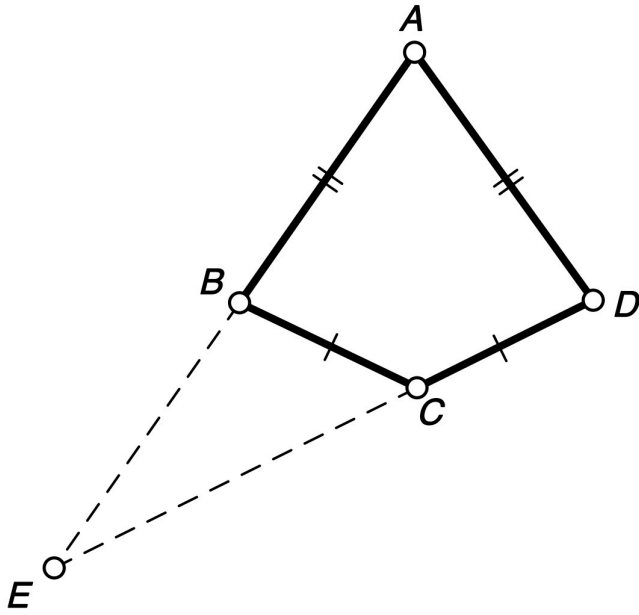
Stanley Rabinowitz, December 2019



$BA=AC$, $BA \perp AC$
 D is the incenter of $\triangle BAC$.

Prove: $DA+AB=BC$

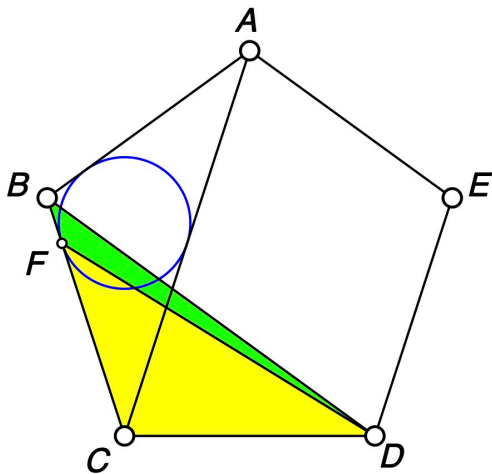
Stanley Rabinowitz, December 2019



$AB=AD, CB=CD$

Prove: $AB \cdot CE=AE \cdot BC$

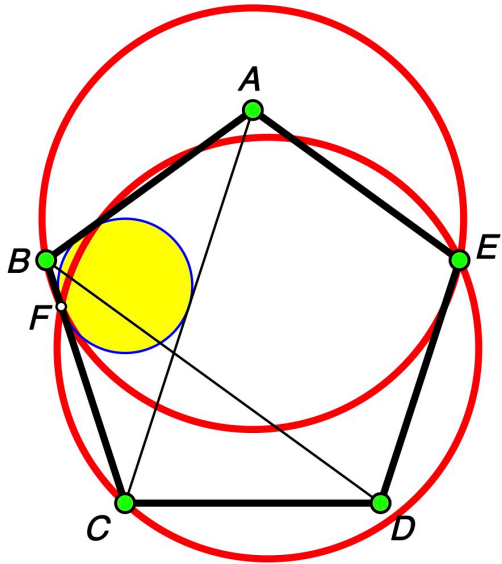
Stanley Rabinowitz, December 2019



ABCDE is a regular pentagon.
F is a touch point.

Prove: Green and yellow triangles
have the same perimeter.

Stanley Rabinowitz, January 2020

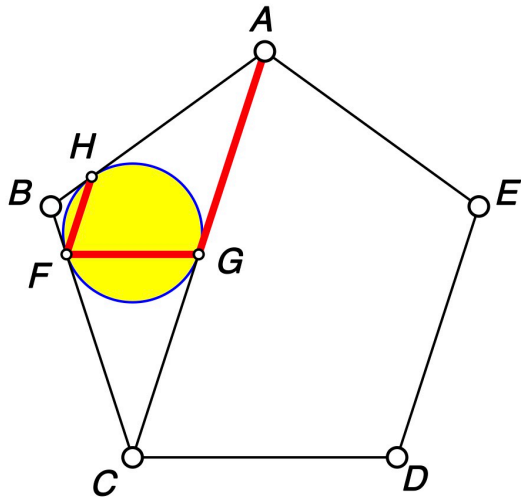


ABCDE is a regular pentagon.
F is a touch point.

Prove:

$\odot BEF$ and $\odot CEF$ are congruent.

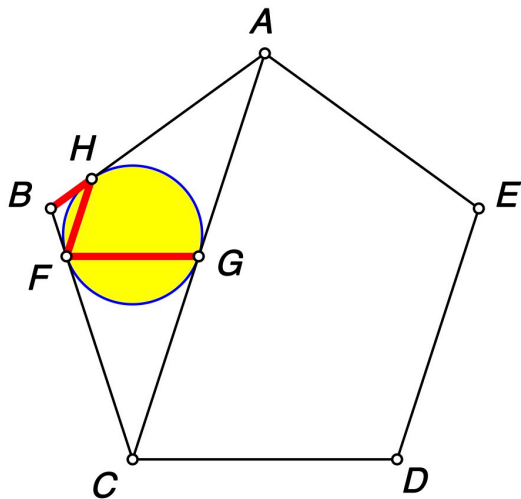
Stanley Rabinowitz, January 2020



ABCDE is a regular pentagon.
F, G, H are touch points.

Prove: $HF + FG = GA$

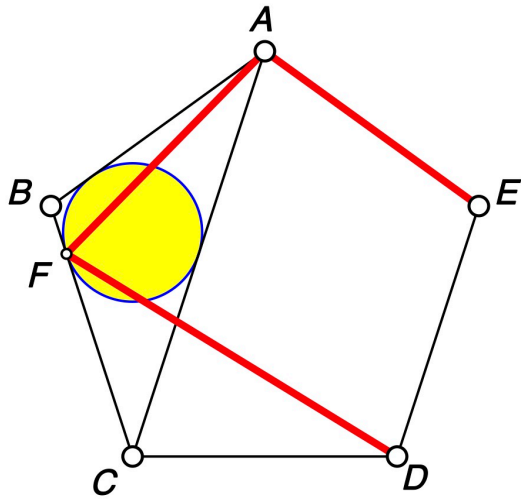
Stanley Rabinowitz, January 2020



ABCDE is a regular pentagon.
F, G, H are touch points.

Prove: $BH + HF = FG$

Stanley Rabinowitz, January 2020



ABCDE is a regular pentagon.
F is a touch point.

Prove: $AE^2 + AF^2 = DF^2$

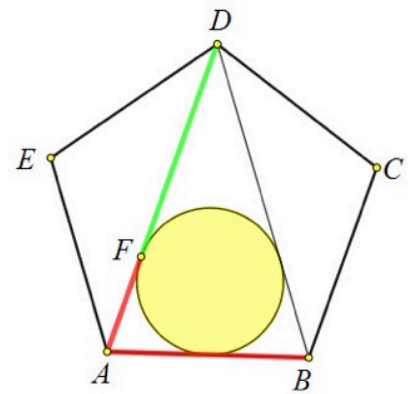
Stanley Rabinowitz, January 2020

4274

★ *ABCDE* regular pentagon

★ *F* touch point

Prove that: $AB^2 + AF^2 = FD^2$



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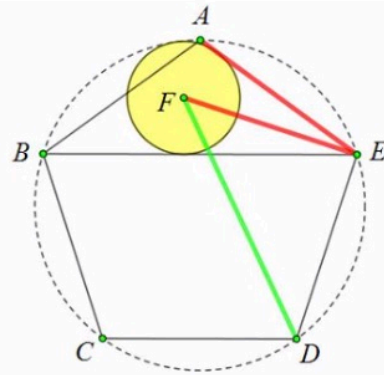


4275

★ $ABCDE$ regular pentagon

★ F incenter of mixtilinear triangle AEB

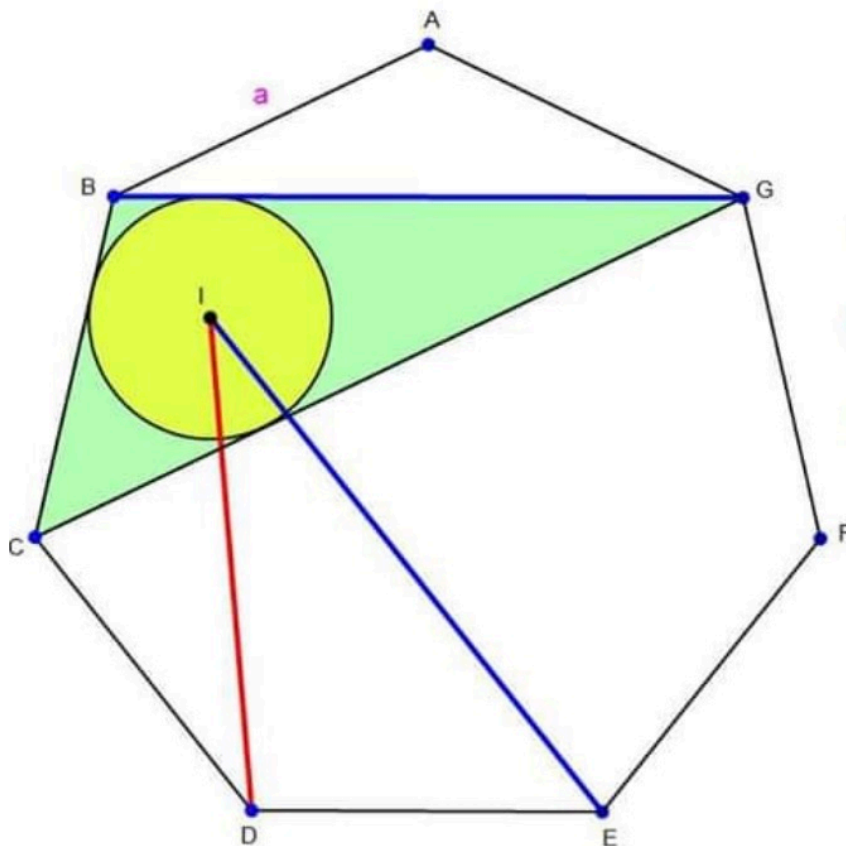
Prove that: $AE^2 + EF^2 = DF^2$



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4280 by Kadir Altıntaş

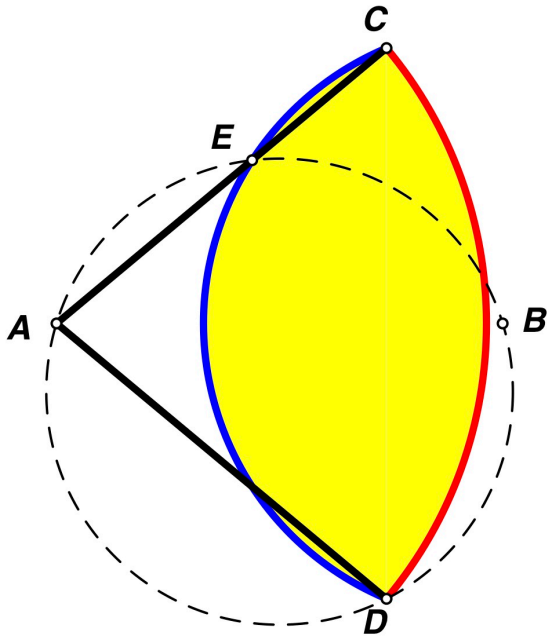


ABC..G regular heptagon, $AB=a$
BGC heptagonal triangle
I incenter of BCG

Prove.

1. Blue segments are equal. i.e. $BG=IE$

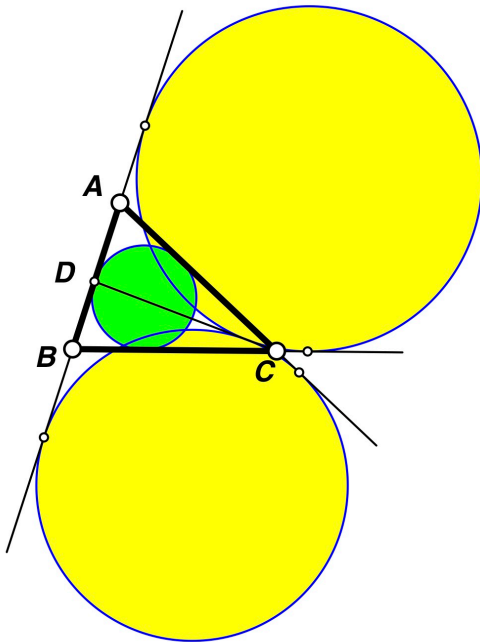
2. $ID= a\sqrt{2}$



**Blue arc is centered at B.
Red arc is centered at A.
AC meets blue arc at E.**

Prove: A, E, B, D concyclic.

Stanley Rabinowitz, January 2020

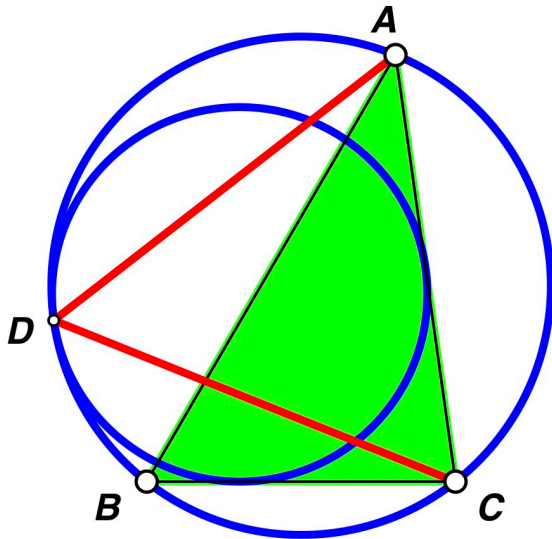


Let D be the point where the incircle of $\triangle ABC$ touches AB.

Prove that the A-excircle of $\triangle DAC$ is tangent to the B-excircle of $\triangle DBC$.

Extra credit: For a fixed $\triangle ABC$, find all points D with this property.

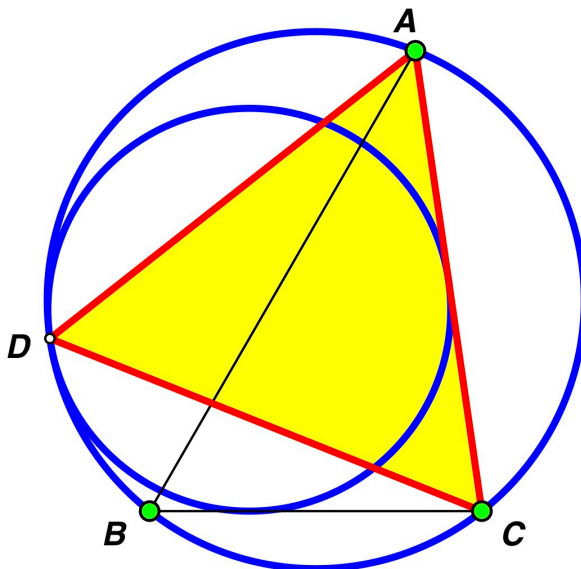
Stanley Rabinowitz, February 2020



$AB + AC = 3 \cdot BC$.
Blue circles touch at D.

Prove: $AD = CD$

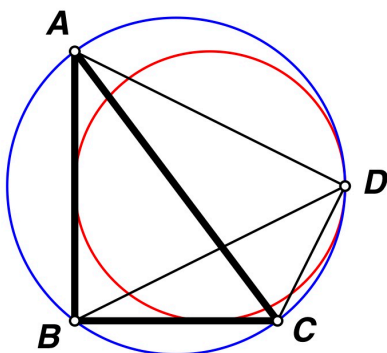
Stanley Rabinowitz, February 2020



$BC=5, AC=7, AB=8$.
Blue circles touch at D.

Prove: $\triangle ACD$ is equilateral

Stanley Rabinowitz, February 2020



$BC=3, AB=4, AC=5$
D is the B-mixtilinear touch point.

Prove that triangles ABD and ACD have the same Euler line.

Stanley Rabinowitz, April 2020